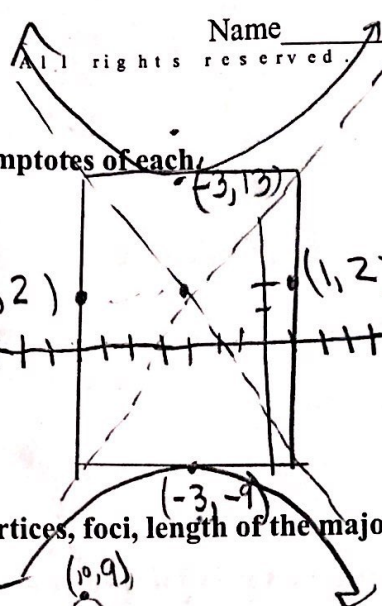


$$y = \frac{11}{4}(x+3) + 2 \rightarrow \frac{11}{4}x + \frac{33}{4} + \frac{2}{1} \rightarrow \frac{11}{4}x + \frac{33}{4} + \frac{8}{4} \quad \boxed{y = \frac{11}{4}x + \frac{41}{4}}$$



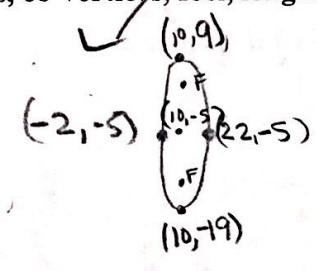
Identify the vertices, foci, and asymptotes of each.

1)  $\frac{(y-2)^2}{121} - \frac{(x+3)^2}{16} = 1$   
 $C(-3, 2)$   
 $a=11$   
 $b=4$   
 $c = \sqrt{121+16}$   
 $c = \sqrt{137}$

$V(-3, 13) (-3, -9)$   
**Foci  $(-3, 2 \pm \sqrt{137})$**   
 Asymptotes  
 $y = \pm \frac{11}{4}(x+3) + 2$

Identify the center, vertices, co-vertices, foci, length of the major axis, and length of the minor axis of each.

2)  $\frac{(x-10)^2}{144} + \frac{(y+5)^2}{196} = 1$   
 $C(10, -5)$   
 $a=14$   
 $b=12$

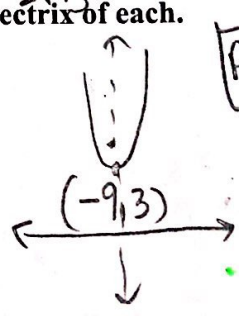


**F  $(10, -5 \pm 2\sqrt{13})$**   
 Length of major axis = 28 units  
 Length of minor axis = 24 units

Identify the vertex, focus, axis of symmetry, and directrix of each.

3)  $y = 7(x+9)^2 + 3$   
 $V(-9, 3)$   
 $F(-9, 3 + \frac{1}{28})$   
 $F(-9, 3 - \frac{1}{28})$

$\frac{1}{4p} = \frac{1}{7}$   
 $28p = 1$   
 $p = \frac{1}{28}$



**AOS:  $x = -9$**   
 directrix  
 $y = 3 - \frac{1}{28}$   
 $\frac{84}{28} - \frac{1}{28}$   
 $y = \frac{83}{28}$

Identify the center and radius of each.

4)  $(x-5)^2 + (y+11)^2 = 24$   
 $C(5, -11)$   
 $r = \sqrt{24}$   
 $r = 2\sqrt{6}$

Identify the conic and write the standard form equation of each.

5) **ellipse**  
 $x^2 - 14x + 49 + 4(y^2 + 10y + 25) = -5 + 49 + 100$   
 $\frac{(x-7)^2}{144} + \frac{4(y+5)^2}{144} = \frac{144}{144}$   
 $\frac{(x-7)^2}{144} + \frac{(y+5)^2}{36} = 1$

6)  $x^2 + y^2 + 30x - 20y + 316 = 0$   
 $x^2 + 30x + 225 + y^2 - 20y + 100 = -316 + 225 + 100$   
 $(x+15)^2 + (y-10)^2 = 9$   
**circle**



$$x^2 + 12x + 36 - 4(y^2 + 4y + 4) = 80 + 36 - 16$$

$$\frac{(x+6)^2}{100} - \frac{4(y+2)^2}{100} = 100$$

$$7) x^2 - 4y^2 + 12x - 16y - 80 = 0$$

$$x - 154 = 3y^2 - 42y$$

$$x - 154 = 3(y^2 - 14y + \dots)$$

$$8) -3y^2 + x + 42y - 154 = 0$$

$$x - 154 + 147 = 3(y^2 - 14y + 49)$$

$$x - 7 = 3(y - 7)^2$$

$$x = 3(y - 7)^2 + 7$$

parabola

$$\frac{(x+6)^2}{100} - \frac{(y+2)^2}{25} = 1$$

hyperbola

Use the information provided to write the standard form equation of each circle.

9) Center:  $(-1, -4)$   
Radius:  $\sqrt{95}$

$$(x+1)^2 + (y+4)^2 = 95$$

$$p = F - V$$

Use the information provided to write the vertex form equation of each parabola.

10) Vertex:  $(5, -6)$ , Focus:  $(5, -5)$

$$p = -5 - (-6) = 1$$

$$y = \frac{1}{4}(x - 5)^2 - 6$$

$$\frac{1}{4p} = \frac{1}{4}$$

11) Focus:  $(-\frac{49}{8}, 7)$ , Directrix:  $x = -\frac{47}{8}$

$$\text{Vertex } (\frac{-49}{8}, 7)$$

$$-\frac{49}{8} + \frac{-47}{8} = -\frac{96}{8} = -12$$

$$V(-6, 7)$$

$$x = \frac{1}{4p}(y - k) + h$$

$$p = V - D = -6 - (-\frac{47}{8}) = -6 + \frac{47}{8} = -\frac{48}{8} + \frac{47}{8} = -\frac{1}{8}$$

$$x = -2(y - 7)^2 - 6$$

Use the information provided to write the standard form equation of each ellipse.

12) Vertices:  $(9, 4), (-13, 4)$   
Co-vertices:  $(-2, 12), (-2, -4)$

$$\frac{(x+2)^2}{121} + \frac{(y-4)^2}{64} = 1$$

13) Foci:  $(-8, -4 + 5\sqrt{3}), (-8, -4 - 5\sqrt{3})$   
Co-vertices:  $(3, -4), (-19, -4)$

$$c = 5\sqrt{3}$$

$$75 = a^2 - 121$$

$$196 = a^2$$

$$\frac{(x+8)^2}{121} + \frac{(y+4)^2}{196} = 1$$

Use the information provided to write the standard form equation of each hyperbola.

14) Vertices:  $(10, 11), (10, -7)$   
Foci:  $(10, 2 + \sqrt{202}), (10, 2 - \sqrt{202})$

$$\text{center } (10, \frac{11 + (-7)}{2}) = (10, 2)$$

$$a = 9, c = \sqrt{202}$$

$$202 = 81 + b^2$$

$$121 = b^2$$

$$\frac{(y-2)^2}{81} - \frac{(x-10)^2}{121} = 1$$

15) Vertices:  $(2, 9), (-8, 9)$   
Perimeter of Central Rectangle = 44

$$C(-3, 9)$$

$$a = 5, b = 6$$

$$\frac{(x+3)^2}{25} - \frac{(y-9)^2}{36} = 1$$

Identify the vertices, foci, and asymptotes of each.

16)  $\frac{(x+7)^2}{196} - \frac{(y-9)^2}{49} = 1$

$$y = \pm \frac{7}{14}(x+7) + 9$$

$$V(-21, 9), (7, 9)$$

$$y = \frac{1}{2}(x+7) + 9 = \frac{1}{2}x + \frac{7}{2} + \frac{18}{2}$$

$$y = -\frac{1}{2}(x+7) + 9 = -\frac{1}{2}x - \frac{7}{2} + \frac{18}{2}$$

$$y = \frac{1}{2}x + \frac{25}{2}$$

$$y = -\frac{1}{2}x + \frac{11}{2}$$



SBM 2 Benchmark Review 2

Factor each and find all roots.

1)  $x^4 + 9x^2 + 8 = 0$   
 $(x^2 + 1)(x^2 + 8) = 0$   
 $x^2 = -1$        $x^2 = -8$   
 $x = \pm\sqrt{-1}$        $x = \pm\sqrt{-8}$   
 $x = \pm i$        $x = \pm 2i\sqrt{2}$   
 $\{\pm i, \pm 2i\sqrt{2}\}$

2)  $x^4 - 2x^3 - 5x^2 + 10x = 0$   
 $x(x^3 - 2x^2 - 5x + 10) = 0$   
 $x(x^2(x-2) - 5(x-2)) = 0$   
 $x(x^2 - 5)(x-2) = 0$   
 $\{0, \pm\sqrt{5}, 2\}$

3)  $x^3 - 6x^2 + 5x = 0$   
 $x(x^2 - 6x + 5) = 0$   
 $x(x-1)(x-5) = 0$   
 $\{0, 1, 5\}$

4)  $x^6 - 4x^4 - 25x^2 + 100 = 0$   
 $x^4(x^2 - 4) - 25(x^2 - 4) = 0$   
 $(x^4 - 25)(x^2 - 4) = 0$   
 $(x^2 + 5)(x^2 - 5)(x+2)(x-2) = 0$   
 $\{\pm i\sqrt{5}, \pm\sqrt{5}, \pm 2\}$

Write a polynomial function of least degree with integral coefficients that has the given zeros.

5)  $-3, 2 + \sqrt{7}, X = -3$   
 $X + 3 = 0$   
 $x = 2 + \sqrt{7}$   
 $(x-2)^2 = (\sqrt{7})^2$   
 $x^2 - 4x + 4 = 7$   
 $x^2 - 4x - 3 = 0$

	$x^2$	$-4x$	$-3$
$x$	$x^3$	$-4x^2$	$-3x$
$3$	$3x^2$	$-12x$	$-9$

$f(x) = x^3 - x^2 - 15x - 9$

6)  $3 - i, \sqrt{5}$   
 $x = 3 - i$   
 $(x-3)^2 = (-i)^2$   
 $x^2 - 6x + 9 = (-1)^2(i)^2$   
 $x^2 - 6x + 9 = -1$   
 $x^2 - 6x + 10 = 0$

$(x^2 - (\sqrt{5})^2)$   
 $x^2 = 5$   
 $x^2 - 5 = 0$

	$x^2$	$-6x$	$10$
$x^2$	$x^4$	$-6x^3$	$10x^2$
$-5$	$-5x^2$	$30x$	$-50$

$f(x) = x^4 - 6x^3 + 5x^2 + 30x - 50$

7)  $f(x) = x^3 - 3x^2 - 1$

8)  $f(x) = -x^4 + 3x^2 - 2x$

↓ ↓

$x \rightarrow -\infty, f(x) \rightarrow -\infty$

$x \rightarrow \infty, f(x) \rightarrow \infty$

$x \rightarrow -\infty, f(x) \rightarrow -\infty$

$x \rightarrow \infty, f(x) \rightarrow \infty$

# Copy Copy Square multiply Square

Factor each completely. SOAP

9)  $216x^3 - 1$   
 $(6x)^3 - (1)^3$

$(6x - 1)(36x^2 + 6x + 1)$

10)  $2x^3 + 16$   
 $2(x^3 + 8)$

$2(x^3 + 2^3)$

$2(x + 2)(x^2 - 2x + 4)$

11)  $256x^3 - 500$

$4(64x^3 - 125)$

$4((4x)^3 - (5)^3)$

$4(4x - 5)(16x^2 + 20x + 25)$

$4(4x - 5)(16x^2 + 20x + 25)$

12)  $27x^3 + 8$

$(3x)^3 + 2^3$

$(3x + 2)(9x^2 - 6x + 4)$

State the possible rational zeros for each function. Then find all zeros.

13)  $f(x) = 2x^3 - 7x^2 + 2x$   
 $P = \{2, \frac{1}{2}\}$   
 $Q = \{2, \frac{1}{2}\}$

$f(x) = x(2x^2 - 7x + 2)$

$\frac{P}{Q} = 0, \pm \{1, \frac{1}{2}, 2\}$

$x = \frac{-(-7) \pm \sqrt{49 - 4(2)(2)}}{2(2)}$

$\frac{7 \pm \sqrt{49 - 16}}{4} = \left\{ 0, \frac{7 \pm \sqrt{33}}{4} \right\}$

15)  $f(x) = 3x^3 + 7x^2 + 4x + 4$

$P = 4 \{1, 2, 4\}$

$Q = 3 \{1, 3\}$

$\frac{P}{Q} = \pm \left\{ 1, \frac{1}{3}, 2, \frac{2}{3}, 4, \frac{4}{3} \right\}$

$$\begin{array}{r} 3 \ 7 \ 4 \ 4 \\ -2 \ 3 \ 7 \ 4 \ 4 \\ \hline 3 \ 1 \ 2 \ 0 \end{array}$$

$3x^2 + x + 2 = 0$   
 $x = \frac{-1 \pm \sqrt{1 - 4(3)(2)}}{2(3)}$

$x = \frac{-1 \pm \sqrt{-23}}{6}$   
 $\left\{ -2, \frac{-1 \pm i\sqrt{23}}{6} \right\}$

16)  $f(x) = 3x^3 - 7x^2 + 5x - 1$

$P = 1$

$Q = 3 \{1, 3\}$

$\frac{P}{Q} = \pm \left\{ 1, \frac{1}{3} \right\}$

$$\begin{array}{r} 3 \ -7 \ 5 \ -1 \\ \downarrow 3 \ -7 \ 5 \ -1 \\ \hline 3 \ -4 \ 1 \ 0 \end{array}$$

$3x^2 - 4x + 1 = 0$   
 $3x^2 - 3x - x + 1 = 0$   
 $3x(x-1) - 1(x-1) = 0$   
 $(3x-1)(x-1) = 0$   
 $x = \frac{1}{3}, x = 1$

$\left\{ 1 \text{ mult } 2, \frac{1}{3} \right\}$



Simplify. Write "undefined" for expressions that are undefined.

1) 
$$\begin{bmatrix} 6 & -5 & 4 \\ -2 & 5 & 4 \end{bmatrix} \begin{bmatrix} 0 & 0 \\ -6 & -4 \end{bmatrix}$$
 undefined

2) 
$$\begin{bmatrix} 0 \\ -3 \\ 5 \\ -6 \end{bmatrix} + \begin{bmatrix} -4 \\ 4 \\ -2 \\ 0 \end{bmatrix} - \begin{bmatrix} 4 \\ -2 \\ 4 \\ -1 \end{bmatrix} = \begin{bmatrix} -4 \\ 1 \\ 3 \\ -6 \end{bmatrix} - \begin{bmatrix} 4 \\ -2 \\ 4 \\ -1 \end{bmatrix} = \begin{bmatrix} -8 \\ 3 \\ -1 \\ -5 \end{bmatrix}$$

3) 
$$\begin{bmatrix} 4 & -5 \\ -3 & 3 \end{bmatrix} \cdot \begin{bmatrix} 2 & -4 & -4 \\ 6 & -3 & 0 \end{bmatrix} - \begin{bmatrix} 3 & 5 & 0 \\ -2 & 2 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 8-30 & -16+15 & -16+0 \\ 6+18 & 12+9 & 12+0 \end{bmatrix} = \begin{bmatrix} -22 & -1 & -16 \\ 24 & 21 & 12 \end{bmatrix}$$

4) 
$$\begin{bmatrix} 0 & -4 \\ -5 & -3 \\ -6 & -5 \end{bmatrix} \cdot \left( \begin{bmatrix} 6 & 2 \\ -6 & -2 \end{bmatrix} - \begin{bmatrix} -6 & -3 \\ -1 & -2 \end{bmatrix} \right)$$

$$\begin{bmatrix} 10 & -4 \\ -5 & -3 \\ -6 & -5 \end{bmatrix} \cdot \begin{bmatrix} 12 & 5 \\ -5 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 20 & 0 \\ -60+15 & -25+0 \\ -72+25 & -30+0 \end{bmatrix} = \begin{bmatrix} 20 & 0 \\ -45 & -25 \\ -47 & -30 \end{bmatrix}$$

Evaluate each determinant.

5) 
$$\begin{vmatrix} 3 & 0 & 4 & 3 & 0 \\ -5 & -1 & 3 & -5 & -1 \\ -5 & 4 & 0 & -5 & -4 \end{vmatrix}$$

$$(0+0+-80) - (-20+-36+6)$$
  

$$-80 - (-56)$$
  

$$-24$$

$$\begin{vmatrix} -25 & -6 & -16 \\ 14 & 1 & 11 \end{vmatrix}$$

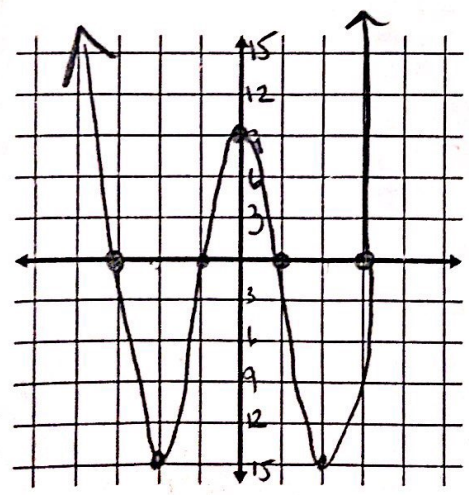
$$\frac{77}{21}$$

6) 
$$\begin{vmatrix} 5 & 2 \\ 2 & -3 \end{vmatrix}$$

$$15 - 4 = 11$$

GRAPH EACH POLYNOMIAL FUNCTION and list all of the characteristics.

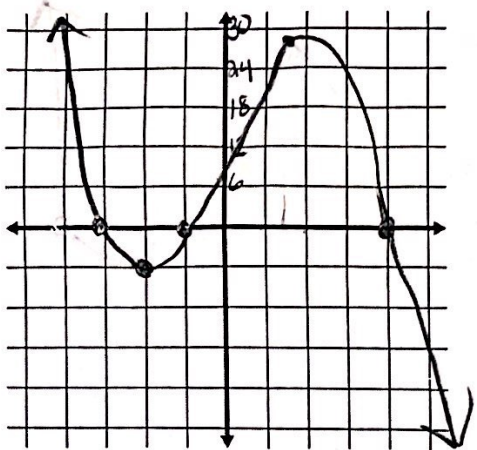
7)  $f(x) = x^4 - 10x^2 + 9$ ; Roots =  $\pm 3, \pm 1$



$f(0) = 9$   
 $f(-2) = -15$   
 $f(2) = -15$

Local Minimum:	$(-2, -15)$ $(2, -15)$
Local Maximum:	$(0, 9)$
Y-Intercept:	$(0, 9)$
End Behavior:	$x \rightarrow -\infty, f(x) \rightarrow \infty$ $x \rightarrow \infty, f(x) \rightarrow \infty$
Domain:	$\mathbb{R}$
Range:	$y \geq -15$
Increase:	$(-2, 0) \cup (2, \infty)$
Decrease:	$(-\infty, -2) \cup (0, 2)$

y's by 6  
 8)  $f(x) = -x^3 + 13x + 12$ ; Roots = -1, 4, -3



Local Minimum:  $(-2, -6)$   
 Local Maximum:  $(1.5, 28.13)$   
 Y-Intercept:  $(0, 12)$   
 End Behavior:  $x \rightarrow -\infty, f(x) \rightarrow \infty$   
 $x \rightarrow \infty, f(x) \rightarrow -\infty$   
 Domain:  $\mathbb{R}$  Range:  $\mathbb{R}$   
 Increase:  $(-2, 1.5)$   
 Decrease:  $(-\infty, -2) \cup (1.5, \infty)$

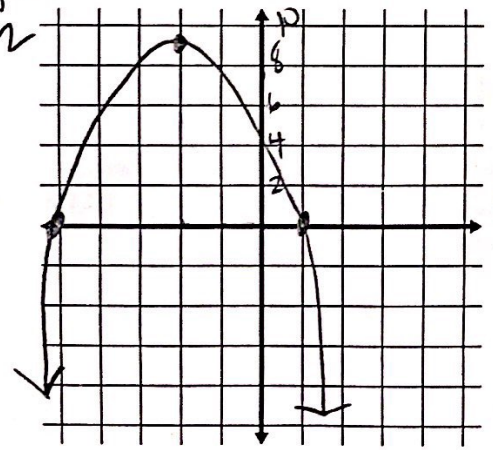
$$\frac{-1+3}{2} = -1$$

$$\frac{-1+4}{2} = 1.5$$

$$f(-2) = -6$$

$$f(1.5) = 28.13$$

y's by 2  
 9)  $f(x) = -x^2 - 4x + 5$ ; Roots = -5, 1



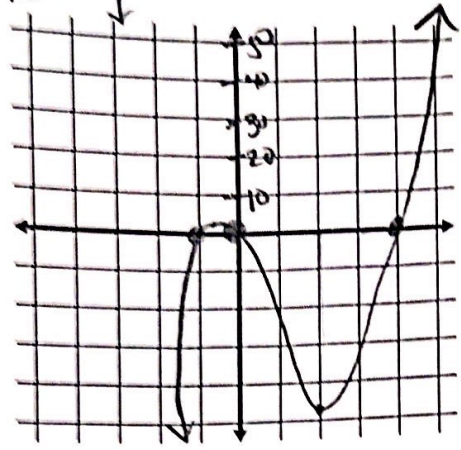
Local Minimum: none  
 Local Maximum:  $(-2, 9)$   
 Y-Intercept:  $(0, 5)$   
 End Behavior:  $x \rightarrow -\infty, f(x) \rightarrow -\infty$   
 $x \rightarrow \infty, f(x) \rightarrow -\infty$   
 Domain:  $\mathbb{R}$  Range:  $y \leq 9$   
 Increase:  $(-\infty, -2)$   
 Decrease:  $(-2, \infty)$

$$\frac{-5+1}{2} = -2$$

$$f(-2) = 9$$



10)  $f(x) = x^5 - 3x^4 - 4x^3$ ; Roots = 0 mult. of 3, -1, 4



Local Minimum:  $(2, -48)$   
 Local Maximum:  $(-0.5, 0.28)$   
 Y-Intercept:  $(0, 0)$   
 End Behavior:  $x \rightarrow -\infty, f(x) \rightarrow -\infty$   
 $x \rightarrow \infty, f(x) \rightarrow \infty$   
 Domain:  $\mathbb{R}$  Range:  $\mathbb{R}$   
 Increase:  $(-\infty, -0.5) \cup (2, \infty)$   
 Decrease:  $(-0.5, 2)$

$f(-0.5) = 0.28$   
 $f(2) = -48$

$P(r) = {}_n C_r p^r q^{n-r}$

11) A coin is flipped 11 times. What is the probability of getting at least 9 heads?

$n = 11$   
 $r = 9, 10, 11$   
 $p = 0.5$   
 $q = 0.5$

$P(9) + P(10) + P(11)$   
 ${}_{11}C_9 (0.5)^9 (0.5)^2 + {}_{11}C_{10} (0.5)^{10} (0.5)^1 + {}_{11}C_{11} (0.5)^{11} (0.5)^0$

0.032714844

12) You just took your science benchmark. Each question had 5 answer choices. What is the probability you got exactly 15 of the 20 questions correct?

$n = 20$   
 $r = 15$   
 $p = .20$   
 $q = .80$

${}_{20}C_{15} (.20)^{15} (.80)^5$   
0.000000166

13) Everyone in your math class of 8 students has taken the driving test. The average passing rate is 81%. What is the probability that more than 1 classmates passed the test?

$n = 8$   
 $r = 2, 3, 4, 5, 6, 7, 8$   
 $p = .81$   
 $q = 0.19$

$P(> 1) = 1 - (P(0) + P(1))$   
 $= 1 - ({}^8C_0 (.81)^0 (.19)^8 + {}^8C_1 (.81)^1 (.19)^7)$   
= 0.999940379